ACTINIDE-RICH AND ACTINIDE-POOR $r$-PROCESS ENHANCED METAL-POOR STARS DO NOT REQUIRE SEPARATE $r$-PROCESS PROGENITORS

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ABSTRACT

The astrophysical production site of the heaviest elements in the universe remains a mystery. Incorporating heavy element signatures of metal-poor, $r$-process enhanced stars into theoretical studies of $r$-process production can offer crucial constraints on the origin of heavy elements. In this study, we introduce and apply the “Actinide-Dilution with Matching” model to a variety of stellar groups ranging from actinide-deficient to actinide-enhanced to empirically characterize $r$-process ejecta mass as a function of election fraction. We find that actinide-boost stars do not indicate the need for a unique and separate $r$-process progenitor. Rather, small variations of neutron richness within the same type of $r$-process event can account for all observed levels of actinide enhancements. The very low-$Y_e$, fission-cycling ejecta of an $r$-process event need only constitute 10–30% of the total ejecta mass to accommodate most actinide abundances of metal-poor stars. We find that our empirical $Y_e$ distributions of ejecta are similar to those inferred from studies of GW170817 mass ejecta ratios, which is consistent with neutron-star mergers being a source of the heavy elements in metal-poor, $r$-process enhanced stars.

Keywords: nuclear reactions, nucleosynthesis, abundances – stars: abundances – stars: Population II – binaries: close

1. INTRODUCTION

The rapid-neutron capture (“$r$”) process is thought to be a main mechanism to synthesize elements heavier than iron and the only mechanism capable of producing the actinide elements, such as thorium and uranium. Astrophysically, possible sites of the $r$-process remain unconfirmed; core-collapse supernovae (CCSNe) and neutron-star mergers (NSMs) are the long-favored candidates. CCSNe were thought to be natural sites for robust $r$-process production since Burbidge et al. (1957). Although several studies have shown that current models of CCSNe cannot reproduce the heavy/main elemental $r$-process pattern of the Solar System, they may still be responsible for the light $r$-process elements (Thielemann et al. 2011; Arcones & Thielemann 2013). The recent NSM event GW170817 (Abbott et al. 2017) and corresponding electromagnetic afterglow AT2017gfo (Kilpatrick et al. 2017; Cowperthwaite et al. 2017; Drout et al. 2017; Shappee et al. 2017) now lends additional observational support for NSMs as robust producers of lanthanide material. Earlier observational evidence in support of NSM was the discovery of the “$r$-process dwarf galaxy” Reticulum II (“Ret II”). In this ultra-faint dwarf galaxy (UFD), high-resolution spectroscopic studies (Ji et al. 2016b; Roederer et al. 2016) identified multiple low-metallicity stars with extreme $r$-process enhancement. Significant $r$-process enrichment in such a small system calls for an event that ejected large amounts of $r$-process material, which Ji et al. (2016a) argue could not be from standard SNe, but could be explained with an NSM. Simulations suggest that one NSM event houses several environments capable of undergoing an $r$-process. Of particular importance are the neutron-rich, low-
entropy dynamical (or tidal) ejecta, which escape at high velocities (Lattimer & Schramm 1974; Meyer 1989; Freiburghaus et al. 1999). On slightly longer timescales is the accretion disk wind, which is estimated to have slightly lower neutron-richness and higher entropy than the tidal ejecta (Surman et al. 2008; Metzger et al. 2008; Perego et al. 2014). Neutrino flavor transformation has the potential to make the wind significantly more neutron rich than currently predicted by simulation (Malkus et al. 2016). An accretion disk wind that may facilitate an r-process is not limited to just NSM environments. Recently, the accretion disk around collapsars—the core-collapse of a massive rotating star—has seen a resurgence as a possible site of robust r-process element production (Pruet et al. 2004; Surman & McLaughlin 2004; Siegel et al. 2018). Other r-process sites have also been proposed, such as magneto-rotational instability-driven SNe (Cameron 2003; Winteler et al. 2012; Nishimura et al. 2015, but see also Mösta et al. 2018), and dark matter-induced neutron star implosions (Bramante & Linden 2016; Fuller et al. 2017).

A well-established method for obtaining empirical evidence on r-process sites is through observations of metal-poor stars in the Milky Way halo that are strongly enriched in r-process elements. The “r-II” stars (defined as [Eu/Fe] > +1.0 and [Ba/Eu] < 0) display a strong relative enhancement of r-process elements in their photospheres compared to their iron content (Barklem et al. 2005; Beers & Christlieb 2005). About 3–5% of stars in the Milky Way halo with [Fe/H] ≲ −2 are classified as r-II, totaling about 30 r-II stars identified as of 2015 (from data in Abdulahaim & Frebel 2017, “JINAbase”). Outside the Milky Way, about ten UFDs had been studied for r-process enrichment as of 2016. At that time, only one—Ret II—was found to have r-II stars, with seven (of nine observed) stars identified as r-II members (Ji et al. 2016b; Roederer et al. 2016). Given the hierarchical merger origin of the Milky Way (Searle & Zinn 1978; Schlaufman et al. 2009; Tumlinson 2010), metal-poor halo stars likely formed in small early galaxies such as analogs of the surviving UFDs. Accordingly, such strong r-process enhancement in halo stars suggests that r-process events occurring in these galaxies, such as NSMs that eject large amounts of r-process material, should overall be favored as early r-process production sites.

Besides the r-II stars, there are also the moderately enhanced “r-I” metal-poor stars (+0.3 < [Eu/Fe] ≤ +1.0 and [Ba/Eu] < 0). These stars possibly formed in somewhat larger dwarf galaxies, such as Tucana III (Hansen et al. 2017), in which the yields of any prolific r-process event would be diluted more than in the case of the formation of r-II stars in smaller systems. The range of both metallicites and level of r-process enrichment at which the r-I and r-II stars are found suggests that NSMs alone could not account for all the r-process material in the Galaxy. As Côté et al. (2018a) argue, it is likely that a separate site (or sites) could have contributed r-process material at early times in the universe.

The r-I and r-II stars show striking similarities in their main r-process patterns among the lanthanide elements (57La through 71Lu). However, some variation exists in the actinide elements, Th and U, with about 30% showing an enhancement of Th relative to the lanthanides (Mashonkina et al. 2014), dubbed the “actinide-boost” stars. There is also a wider variation of the elemental abundances that follow the first r-process peak—Sr, Y, and Zr—with respect to their scaled main r-process abundances (Siqueira Mello et al. 2014; Ji et al. 2016a). Due to these variations, it is thought that Sr–Y–Zr may originate from a different r-process environment than what produces the lanthanides and actinides, such as the limited-r-process, which would primarily synthesize Z < 56 elements (Travaglio et al. 2004; Hansen et al. 2012; Arcones & Thielemann 2013; Wanajo 2013; Frebel 2018). Similarly, the actinide variation may indicate a separate r-process progenitor object or site that is responsible for the existence of actinide-boost stars (Schatz et al. 2002).

Alternatively, it may be possible that the variations in the actinides and limited-r elements in the r-I and r-II stars can be fully accounted for by variations of astrophysical conditions (e.g., the electron fraction, Y_e) within the same r-process source (i.e., type of site). In this work, we identify key elemental abundance measurements of metal-poor r-process enhanced stars to give insight into the progenitor r-process events that gave rise to the observed abundance variations. These key measurements are used in concert with our theoretical “Actinide-Dilution with Matching” model to ascertain whether the existence of actinide-boost stars suggests one distinct r-process site or if the range of (relative) actinide element abundances can be plausibly explained by a continuum of conditions within the same type of source. With this analysis in hand, we are able to weigh in on the implications of the observations of limited-r and actinide elements, and further, to use observations of low-metallicity stars to provide a consistency check on the amount of lanthanide-rich material inferred from recent “kilonova” observations.
In Section 2, we discuss r-process patterns of metal-poor stars and quantify distinct differences in their scaled abundances that could reflect different r-process sites or conditions among the earliest r-process events. In Section 3, we introduce and detail our Actinide-Dilution with Matching model. Next, we apply this model to different groups of r-process enhanced stars that were likely enriched by just one event, and we present these results in Section 4. In Section 5, we investigate variations on the astrophysical and nuclear inputs that could affect our model results. Finally in Section 6, we compare our empirical Y_e distributions of mass ejecta to that of the GW170817 associated kilonova to test if our results align with these recent observations.

2. OBSERVATIONS OF METAL-POOR STARS

In this section, we discuss observations of metal-poor stars in the context of actinide and limited-r production. To study the full range of the elemental r-process pattern at early times, we choose Zr, Dy, and Th as representative of the limited-r process, main r-process, and actinides, respectively. Although 36Sr and 63Eu are traditionally used to quantify the limited-r and main r-process contributions, we instead use 40Zr and 68Dy to probe these two regions. More and unsaturated absorption lines of Zr II are available over the few of Sr II from which to derive an abundance, leading to Zr abundances with higher precision. In addition, Sr II suffers larger systematic abundance corrections from assuming local thermodynamic equilibrium (LTE) over non-LTE, while the Zr II corrections are lower and the abundances more robust under LTE (Andrievsky et al. 2011).

In the lanthanide region, the production of Eu by the r-process may be sensitive to fission yields, especially to broad and asymmetric fission distributions that place material above the second r-process peak (e.g., Kodama & Takahashi 1975; Eichler et al. 2015; Coté et al. 2018b; Vash et al. 2018). Moreover, the fission fragment distributions of nuclei that may participate in the r-process at high nuclear masses are far from known. To avoid fission-dependent results, we use Dy instead of Eu. At a slightly higher mass, Dy is nearly insensitive to the direct effects of fission fragment distributions.

2.1. Milky Way r-Process Enhanced Stars

We first consider all metal-poor Milky Way stars that have both Zr and Dy abundance measurements included in JINAbase and individual additions from the recent discoveries in Placco et al. (2017), Ji & Frebel (2018), Sakari et al. (2018), and Holmbeck et al. (2018). This data set is displayed in the top panel of Figure 1. The absence of stars with both low Zr and high Dy abundances (i.e., upper-left of the top panel of Figure 1) may suggest that some minimum Zr is made in the same event that created Dy. This trend was also noted in Roederer (2013) who analogously used Sr and Ba abundances.

The light and dark blue dashed lines in Figure 1 indicate log ε(Zr/Dy) = 0.95 and log ε(Zr/Dy) = 0.46, respectively, solely for reference and guidance on the abundance trend. Stars with log ε(Zr/Dy) > 0.95 are mostly those with no r-process enhancement (i.e., [Eu/Fe] ≤ +0.3) and/or with enhancement in other elements, such as carbon and s-process elements (e.g., [Ba/Eu] ≥ 0). The line at log ε(Zr/Dy) = 0.46 reflects that of the scaled, average log ε(Zr/Dy) abundance for r-process stars in Ret II. We note that all stars with a Th measurement have a log ε(Zr/Dy) abundance of at least this value. The bottom panel of Fig-
The range of $\log \epsilon(\text{Th}/\text{Dy})$ abundances is entirely represented by stars with $\log \epsilon(\text{Zr}/\text{Dy}) \leq 0.95$. At higher values of $\log \epsilon(\text{Zr}/\text{Dy})$, the $\log \epsilon(\text{Th}/\text{Dy})$ appears to converge towards a constant value of $\log \epsilon(\text{Th}/\text{Dy}) \approx -1.0$.

Most of the confirmed $\tau$-process enhanced stars lie in the range $0.46 \leq \log \epsilon(\text{Zr}/\text{Dy}) \leq 0.95$. These stars also show the broadest range of $\log \epsilon(\text{Th}/\text{Dy})$. For this work, we posit that these $\tau$-process stars display a pure $\tau$-process signature that has come from just one event. For $\tau$-process stars with $\log \epsilon(\text{Zr}/\text{Dy}) > 0.95$, while it is possible that their $\tau$-process signatures may have also come from a single event, it is also possible that their $\tau$-process material has been diluted or altered by additional types of nucleosynthesis (i.e., other than a main $\tau$-process) or strong contributions from limited-$\tau$ process events. Therefore, to study the widest range of actinide production by a single $\tau$-process site, we focus on $\tau$-process stars with $\log \epsilon(\text{Zr}/\text{Dy}) \leq 0.95$.

### 2.2. Kinematically Linked Groups of $\tau$-Process Enhanced Stars

Given the presumed accretion of stars that now reside in the Milky Way’s halo, the $\tau$-process enhanced halo stars have essentially unknown origins. Specifically, it has been suggested that the $\tau$-process enhanced halo stars originated in dwarf galaxies that were eventually accreted by the Milky Way as part of its hierarchical growth. If a prolific $\tau$-process event enriched the original, low-mass host galaxy, such as that in Ret II, the imprints on these stars offer a window into the element production by (presumably) single $\tau$-process events.

Roederer et al. (2018) recently found kinematic grouping among spatially unrelated $\tau$-process enhanced halo stars. These kinematic groups are further evidence that $\tau$-process enhanced halo stars were once members of satellite galaxies which became accreted by the Milky Way. The progenitor dwarf galaxies of these kinematic groups could resemble Ret II, where all stars belonging to each of these progenitor systems would have formed from gas enriched by single, respective $\tau$-process events. Therefore, we assume that the elemental abundances of stars in the kinematic groups now reflect the range of element production by single events. Abundance pattern differences among members of each group could then point to different astrophysical $\tau$-process conditions within the same type of event or even entirely different $\tau$-process sources. In this regard, the seven $\tau$-II stars in Ret II can be treated as an additional such group as it is highly likely that only one $\tau$-process event took place prior to their formation. Hence, stellar abundance variations within these groups could provide insight into the range of $\tau$-process element production by a single event.

In the following, we expand on the principal idea of assigning groups of $\tau$-process stars. Specifically, we focus on elemental abundance variations between these groups in the actinide and limited-$\tau$ elements. Here, we define “actinide-deficient” as $\log \epsilon(\text{Th}/\text{Dy}) < -1.20$, “actinide-normal” as $-1.20 \leq \log \epsilon(\text{Th}/\text{Dy}) \leq -0.90$, and “actinide-boost” as $\log \epsilon(\text{Th}/\text{Dy}) > -0.90$.

**Ret II** — Although the scaled, heavy-element (between Ba and the third peak) abundance patterns of seven Ret II stars closely resemble those of $\tau$-II halo stars, the only Ret II member for which a Th measurement is available (DES J033523−540407; Ji & Frebel 2018) displays a strikingly low actinide abundance compared to its lanthanides ($[\text{Th}/\text{Eu}] = -0.34$). The seven $\tau$-II stars of Ret II might reflect an event with low actinide production, or possibly one with a significant range. Without a complete set of Th abundances for each of the seven stars in Ret II, we assume, for simplicity, that this low actinide level reflects low actinide production in the $\tau$-process event that enriched the Ret II gas. Thus we assume Ret II has $\log \epsilon(\text{Th}/\text{Dy}) = -1.49$.

**Group F** — The kinematic “Group F” in Roederer et al. (2018) consists of three stars: CS 29529-054 (Roederer et al. 2014a, b), HE 2224+0143 (Barklem et al. 2005; Ren et al. 2012), and HD115444 (Westin et al. 2000), the latter two of which have “normal” actinide abundances: $[\text{Th}/\text{Eu}] = 0.05$ and $[\text{Th}/\text{Eu}] = -0.21$, respectively, and $\log \epsilon(\text{Th}/\text{Dy}) = -1.19$ on average.

J0954+5246 — Just a single star, but representing extreme levels of actinide production by an $\tau$-process.

2MASS J09544277+5246414 (“J0954+5246”; Holmbeck et al. 2018) is currently the most actinide-enhanced $\tau$-II star known, with $[\text{Th}/\text{Eu}] = 0.38$ and $\log \epsilon(\text{Th}/\text{Dy}) = -0.65$.

We treat these three levels of relative actinide enhancement as three distinct “groups” and assume that each group’s members formed from gas enriched by a individual $\tau$-process event. Together, the stellar abundances of the stars in Ret II ($N = 7$), Group F ($N = 3$), and J0954+5246 ($N = 1$) reflect a range of actinide enhancement, which may indicate either separate $\tau$-process actinide sources or a variation within one type of $\tau$-process source.

Between the three groups, the abundances of the limited-$\tau$ elements (Sr, Y, and Zr) also vary with respect to the lanthanide abundances. Whereas it has been suggested that these light neutron-capture elements may originate from a separate $\tau$-process site, we assume in this analysis that for $\tau$-process enhanced stars with $\log \epsilon(\text{Zr}/\text{Dy}) \leq 0.95$, these elements come from the
we build empirical r-process ejecta distributions as a function of $Y_E$ by employing a Monte-Carlo method as an extension to the Actinide-Dilution (“AD”) model introduced in Holmbeck et al. (2019), which we call the Actinide-Dilution with Matching (“ADM”) model. To constrain the model by matching results to stellar abundances, we use three particular regions of the observed $r$-process elemental abundance patterns: the limited- $r$ group, the lanthanides, and the actinides, represented by Zr, Dy, and Th, respectively. These abundance constraints and their allowed tolerances for the ADM model results are listed in Table 1 when using the three groups described in Section 2.2.

Since Th could only be measured in one or two stars per group, the allowed abundance ratios listed in Table 1 come from a single star with the assumption that all other stars within the group have log $\epsilon$(Th/Dy) ratios lying with a broad 0.3 dex of that single measurement. Furthermore, we add 0.2 dex to the adopted log $\epsilon$(Th/Dy) matching-constraint listed in Table 1. This addition accounts for radioactive Th decay over roughly 10 Gyr from the final abundances of our r-process calculations to the present.

Of the three groups in Figure 2, only one star has a reliable uranium measurement, which is unsurprising given that overall, fewer than ten r-process enhanced stars have a reliable detection of uranium. For stars with both Th and U measurements available, studies applying radioactive decay dating have shown the U/Th production ratio to be roughly constant, log $\epsilon$(U/Th) $\approx -0.25$, even for the actinide-boost stars which show absolute enhancement in these elements (e.g., Cowan et al. 1999; Schatz et al. 2002; Wanajo et al. 2002; Farouqi et al. 2010). Hence, for this analysis, we assume that the r-process material in all stars with Th was produced with the same U/Th ratio, and supply this ratio as an additional constraint to the ADM model. The production ratio rather than the observed ratio is used since Th and U are radioactive, and their abundances change over time.

After establishing the observational constraints, we first ran several r-process simulations using a medium-entropy parameterized trajectory (evolution of an ejecta mass element, here with initial entropy $s/k \approx 40$ and
dynamical timescale $\tau_{\text{dyn}} = 20$ ms) as in Zhu et al. (2018). This trajectory is consistent with an accretion disk wind around a proto-neutron star (e.g., a collapsar or NSM remnant; Surman & McLaughlin 2004). We vary the $Y_e$ as in Holmbeck et al. (2019) to allow for multiple levels of neutron-richness within the same environment, changing the initial $Y_e$ from 0.005 to 0.450 in equal steps of 0.005. The $r$-process calculations are run using the nuclear network code Portable Routines for Integrated nucleoSynthesis Modeling (PRISM; Mumpower et al. 2017; Côté et al. 2018b; Mumpower et al. 2018; Vassh et al. 2018). Reaction and decay rates relevant to the $r$-process are constructed as self-consistently as possible. Starting with nuclear masses from the Finite Range Droplet Model (FRDM2012; Möller et al. 2012, 2016), we adopt the neutron-capture and neutron-induced fission rates calculated self-consistently with FRDM2012 masses using the Los Alamos National Laboratory statistical Hauser-Feshbach code (Kawano et al. 2016). The QRPA+HF framework (Mumpower et al. 2016) is used to calculate the relative probabilities of $\beta$-decay, $\beta$-delayed fission, and $\beta$-delayed neutron emission for each nucleus, using Möller et al. (2018) $\beta$-decay strength functions. Fission barrier heights from Möller et al. (2015) are used to calculate fission rates, employing the Zagrebaev et al. (2011) relation for the spontaneous fission channel and adopting symmetric fission fragment distributions for all fission channels.

Figure 3 shows the final calculated Zr, Dy, and Th abundances as functions of $Y_e$. At the highest values of $Y_e$ considered, a large amount of limited-$r$ material around the first peak (here Zr) is synthesized, yet material does not move much beyond the second $r$-process peak ($A \approx 130$, $Z \approx 54$) until $Y_e < 0.30$. With decreasing $Y_e$, the lanthanides (Dy) are produced, and actinide production begins at $Y_e < 0.23$. The oscillatory behavior of the lanthanide and actinide abundances at very low $Y_e$ are due to fission cycles that occur in very neutron-rich environments (as discussed in detail in Holmbeck et al. 2019).

With final abundances generated as functions of $Y_e$, we randomly select fifteen $Y_e$’s between 0.005 and 0.450 and the corresponding final Zr, Dy, Th, and U abundances. Next we add the total Zr, Dy, Th, and U abundances over the fifteen randomly selected values. If the total $\log \epsilon$(Zr/Dy), $\log \epsilon$(Th/Dy), and $\log \epsilon$(U/Th) abundances are within the specified constraints of Table 1, we keep all fifteen $Y_e$’s. We repeat this sampling until we accumulate 100 successes, summing a total of 1500 individual abundance patterns. When combined, the summed abundances pattern matches the relative observational Zr, Dy, Th, and U abundances for a given kinematic group within the listed tolerances.

4. ADM MODEL RESULTS

Figure 4 shows the empirical $r$-process ejecta distribution results of the ADM model applied to the three stellar cases discussed in Section 2.2. The empirical mass ejecta distributions that characterize the observed abundance ratios of Ret II, Group F, and J0954+5246 mainly differ in the very low-$Y_e$ tail ($Y_e < 0.18$ in this trajectory) where robust fission cycling and actinide production occurs. The low actinide abundance constraints of the Ret II group allows less mass in this very low-$Y_e$ tail to be ejected, while the actinide-normal Group F and
actinide-boost J0954+5246 allow increasing amounts of this fission-cycled material.

The bulk of the mass of material (at $Y_e \geq 0.18$) maintains a similar shape in all three cases, including a strong preference for $Y_e \approx 0.25$ and a dip in ejecta production at $Y_e \approx 0.18$. The peak occurs because the log $\epsilon$(Th/Dy) ratio is satisfied near $Y_e \approx 0.25$ for all three cases. On the other hand, the dip at $Y_e \approx 0.18$ coincides with maximal actinide production and (locally) minimal lanthanide production when using this trajectory (see Figure 3), producing a log $\epsilon$(Th/Dy) ratio that is much higher than what observations suggest.

Figure 5 shows the final abundance patterns for the ejecta distributions shown in Figure 4. Every individual abundance pattern (blue) represents a successful set of the fifteen random $Y_e$ choices made in the ADM method. Each combined abundance pattern (red) succeeds in reproducing the scaled abundances of the limited-$r$ elements and many of the lanthanide elements. The common dip surrounding $Z = 60$ (Nd) is mostly due to the strong shell closures of FRDM2012, and partially due to the pure symmetric fission fragment yields we employ. However, this underproduction does not have any influence over the results we present here. We finally note that for all three stellar groups, we have only supplied three abundance constraints to the ADM model. Hence, with few constraints, relatively good agreements across the entire $r$-process patterns are produced.

4.1. The Low-$Y_e$ Component

The largest difference in the empirical $Y_e$ distributions of ejecta with varying levels of actinide enhancement lies in the allowed mass produced in very low-$Y_e$ environments. To investigate this difference in detail, we systematically vary the ADM model input log $\epsilon$(Th/Dy) constraint while holding the log $\epsilon$(Zr/Dy) constraint constant. This way, we can quantify the amount of very low-$Y_e$ material that the progenitor $r$-process event may eject. We repeat this process twice, once holding the log $\epsilon$(Zr/Dy) constraint at 0.46 and again at 0.95, following the labeled bounds in Figure 1 (top panel). Recall that these bounds contain $r$-process enhanced stars in which the $r$-process material likely originated from one $r$-process event. These systematic results are also compared to ADM results using both the log $\epsilon$(Th/Dy) and log $\epsilon$(Zr/Dy) observational abundance ratios from single $r$-process enhanced stars in the bottom panel of Figure 1.

Systematically varying the log $\epsilon$(Th/Dy) input constraint shows a smoothly increasing fraction of allowed ejecta masses at very low-$Y_e$. The $r$-process enhanced stars with likely single $r$-process progenitors fall between the two calculated curves (blue solid and dashed lines) in Figure 6, by definition. Most of these stars thus allow about 10% to 25% of their progenitor’s $r$-process ejecta mass to be at $Y_e < 0.18$. The actinide-boost stars found at log $\epsilon$(Th/Dy) $> -0.90$ allow roughly 25% to 35% of this very low-$Y_e$ material. This enhancement accounts for increased actinide abundances. Stars falling below the lower curve are those with higher log $\epsilon$(Zr/Dy).
mass fraction $Y_e$ component (%)

$\log(\epsilon(Zr/Dy)) = 0.46$
$\log(\epsilon(Zr/Dy)) = 0.95$
$\log(\epsilon(Zr/Dy)) = \text{obs.}$

![Figure 6. Percentage of allowed very low $Y_e$ (<0.18), actinide-rich mass to reproduce various $\log(\epsilon(Th/Dy))$ abundances, while requiring the specified $\log(\epsilon(Zr/Dy))$ ratio. Gray dots show the ADM model applied to select $r$-process stars with observed $\log(\epsilon(Zr/Dy))$ and $\log(\epsilon(Th/Dy))$ ratios as input constraints (Abohlama & Frebel 2017; Placco et al. 2017; Sakari et al. 2018; Holmbeck et al. 2018).](image)

ratios, which formed from gas that was likely polluted by multiple events. Assuming the $r$-process signature in stars with higher $\log(\epsilon(Zr/Dy))$ originated from a single event, the ADM model can then account for their observed $r$-process element distributions using a mass ejecta distribution that is shifted to higher-$Y_e$ values.

Our ADM model results do not indicate a clear separation between the actinide-boost stars and their non-actinide-enhanced counterparts. This agrees with the observed actinide abundances which suggest a smooth distribution of actinide enhancements, with the actinide-boost stars populating a low-probability tail of this distribution. This indicates that the same $r$-process source can produce all levels of actinide enrichment seen in $r$-process enhanced stars. Different levels of actinide enhancement would then reflect a slightly different distribution in the mass ejecta properties within the $r$-process progenitor. In all cases, the amount of fission-cycled (in this trajectory, $Y_e < 0.18$) material required to reproduce our $r$-process abundance observations may be a significant—but not dominant—fraction of the entire $r$-process mass ejecta since it sensitively affects the actinide contribution.

Interestingly, the abundance ratios can still be reproduced by the ADM model when the very low-$Y_e$ component is omitted entirely. We investigate this effect by repeating the ADM calculation, only allowing the model to sample at $0.45 \leq Y_e \leq 0.18$. These results are shown in Figure 7. Disallowing $Y_e$ below 0.18 produces a somewhat bimodal distribution driven by the

log $\epsilon(Zr/Dy)$ and log $\epsilon(Th/Dy)$ requirements. For Ret II and Group F, a peak forms at $Y_e \approx 0.25$, coinciding with the single $Y_e$ that satisfies the input $\log(\epsilon(Th/Dy))$ ratio. Since no Th can come from $Y_e < 0.18$, all the Th contribution is concentrated around this $Y_e$. However, for the actinide-boost case, not enough Th is produced at $Y_e \approx 0.25$, and the ejecta mass builds up near the cutoff at $Y_e = 0.18$ where actinides are still able to be synthesized at levels necessary to eventually reproduce observed stellar abundances, within the allowed ranges of Table 1. With the total amount of Dy constrained mostly by contributions from the $Y_e = 0.25$ region, the Zr abundance primarily comes from higher values of $Y_e$. This restraint produces the broad peak around $Y_e = 0.37$. Although these precise $Y_e$ constraints are mildly dependent on other astrophysical parameters (discussed in Section 5), we conclude that it is possible to reproduce the abundance patterns seen in $r$-process enhanced stars without fission cycling (for the conditions considered here, meaning without $Y_e < 0.23$ material), but such a cutoff places stricter and more finely tuned requirements on the distribution of $Y_e$ in the ejecta.

The ADM model would fail for Ret II if a $Y_e$ cutoff of 0.23 or greater was applied because there is simply not enough actinide material produced. Similarly, applying a cutoff at $Y_e \geq 0.21$ would prevent the ADM model from reproducing actinide-boost abundance ratios. As seen in Figure 3, the Th abundance rises rapidly as $Y_e$ decreases from 0.24 to 0.17, covering over four dex—and thus all observed levels—of actinide abundance. It is therefore unsurprising that the ADM model consistently favors this range. Next, we turn to the higher $Y_e$ component which contributes the bulk of the ejected Zr (i.e., limited-$r$) material.
4.2. The Higher-\(Y_e\) Component

In analogy to Figure 6 of the very low-\(Y_e\) component fraction, Figure 8 shows the allowed fraction of material ejected at \(Y_e > 0.30\) as a function of the input log \(\epsilon(\text{Zr/Dy})\) to characterize the limited-\(r\)-process contribution from single \(r\)-process events. The ADM model is run multiple times varying the input log \(\epsilon(\text{Zr/Dy})\) while holding the log \(\epsilon(\text{Th/Dy})\) constant, first at the actinide-boost cutoff (\(\epsilon(\text{Th/Dy}) = -0.90\)) and then at the very actinide-poor value following Ret II (\(\epsilon(\text{Th/Dy}) = -1.49\)). The ejecta mass fraction with \(Y_e > 0.30\) is also shown for individual stars using their observational log \(\epsilon(\text{Zr/Dy})\) and log \(\epsilon(\text{Th/Dy})\) abundance ratios as constraints.

Figure 8 suggests that in order for the \(r\)-process event to synthesize all the required limited-\(r\)-material as well as the main \(r\)-process material, a minimum of roughly 25% of the mass must be ejected at \(0.30 < Y_e \leq 0.45\). For stars with log \(\epsilon(\text{Zr/Dy}) \leq 0.95\) which likely received their \(r\)-process material from only one progenitor—between roughly 25% and 35% of the progenitor ejecta mass has \(0.30 < Y_e \leq 0.45\). Furthermore, because there is an observational minimum of log \(\epsilon(\text{Zr/Dy}) \approx 0.46\), our ADM model results imply that at least ~25% of the \(r\)-process ejecta mass must be ejected at these higher values of \(Y_e\).

If the material in stars with log \(\epsilon(\text{Zr/Dy}) > 0.95\) were to originate from a single \(r\)-process progenitor, then more than 40% of the \(r\)-process ejecta must be at \(Y_e > 0.30\). However, as previously noted, the main \(r\)-process material found in stars moderately enhanced in \(r\)-process elements with log \(\epsilon(\text{Zr/Dy}) > 0.95\) could have been diluted by limited-\(r\)-only events such as CCSN neutrino-driven winds that primarily produce the limited \(r\)-process elements (Arcones & Thielemann 2013; Wanajo 2013).

5. MODEL VARIATIONS

In this section, we investigate the impact that both astrophysical and nuclear physics variations have on the results of our ADM model to test the robustness of these empirically built mass ejecta distributions.

5.1. Astrophysical Sites

The previous calculations only consider the \(r\)-process originating from a single site: an accretion disk wind. Two situations that might occur in "realistic" astrophysical \(r\)-process events are a mix of ejecta types and a mix of different entropies. One promising \(r\)-process production site is the very low-\(Y_e\) tidal ejecta of an NSM. We choose a low-entropy \((s/k \approx 10)\) trajectory from the 1.4–1.4 \(M_\odot\) NSM simulations by S. Rosswog as in Korobkin et al. (2012) for the tidal ejecta. Next, we vary the initial \(Y_e\) between 0.005 and 0.180 and run full \(r\)-process calculations for this tidal ejecta trajectory. Then we used the ADM model to randomly sample from only the tidal ejecta component at \(Y_e < 0.13\), and from only the wind component at \(Y_e \geq 0.18\). For the region at \(0.13 \leq Y_e < 0.18\), the ADM model samples from both the tidal and wind ejecta with equal probability, producing a mixed-ejecta distribution. This combination may

\begin{figure}
\centering
\includegraphics[width=0.8\textwidth]{figure8.pdf}
\caption{Percentage of allowed \(Y_e > 0.30\), Zr-rich mass to reproduce various log \(\epsilon(\text{Zr/Dy})\) abundances with constant log \(\epsilon(\text{Th/Dy})\) ratio constraints. Gray dots show the ADM model applied to select \(r\)-process stars with their observed log \(\epsilon(\text{Zr/Dy})\) and log \(\epsilon(\text{Th/Dy})\) ratios as input constraints (Abohalima & Frebel 2017; Placco et al. 2017; Sakari et al. 2018; Holmbeck et al. 2018), with red circles denoting the actinide-boost stars.}
\end{figure}

\begin{figure}
\centering
\includegraphics[width=0.8\textwidth]{figure9.pdf}
\caption{Ejecta distribution predicted by the ADM model matching Ret II abundances using the disk wind trajectory only ("wind"), an NSM represented by a combination of wind and tidal ejecta ("ejecta mix"), and a combination of different entropies ("entropy mix"). All simulations use the FRDM2012 mass model.}
\end{figure}
be one representation of total NSM ejecta undergoing an $r$-process. Figure 9 shows the empirical $Y_e$ distribution obtained by using a combination of wind and tidal ejecta which match the Ret II abundances (“ejecta mix”). Although the $Y_e < 0.18$ component is distributed differently in the mixed ejecta case than the wind-only counterpart, the amount of necessary $Y_e < 0.18$ mass from the tidal ejecta is similar to that of the wind.

The $r$-process can also feasibly occur in an environment that supports a range of entropies. We investigate the effect of entropy on the $Y_e$ distribution by repeating the simulations with a high entropy ($s/k \approx 85$) trajectory for the entire range of $0.005 \leq Y_e \leq 0.450$ in equal steps, and extended the very low entropy tidal trajectory to $Y_e \leq 0.250$. Next, the ADM model was run, randomly sampling between the original disk wind trajectory and the high entropy trajectory for $0.250 < Y_e \leq 0.450$, and between the low, medium, and high entropy trajectories for $0.005 \leq Y_e \leq 0.250$. The ejecta distribution results from the ADM model using a random combination of entropies are shown in Figure 9 (“entropy mix”).

The previously mentioned dip at $Y_e \approx 0.18$ disappears when combining trajectories with different astrophysical properties. This is because the value $Y_e = 0.18$ does not universally signify robust actinide production for all $r$-process trajectories. In the lowest entropy (tidal ejecta) trajectory, the Th abundance peaks at the lower $Y_e$ of 0.125. At $Y_e = 0.18$, instead of a peak in Th production occurring—as that produced by the high and medium entropy (wind) trajectories—the very low-entropy tidal ejecta trajectory produces a Dy peak, allowing the mass at $Y_e \approx 0.18$ to satisfy the input abundance ratio constraints and wash out the apparent two-component $Y_e$ distribution.

In summary, considering variations in the astrophysical site slightly affects the details of the predicted ejecta mass distribution. However, qualitatively, the ADM model robustly suggests that if there is any low-$Y_e$ fission cycling ejecta component, it must be small compared to the $r$-process material ejected by the disk wind at higher $Y_e$.

5.2. Nuclear Physics Inputs

Nucleosynthesis calculations of the $r$-process rely heavily on theoretical data to attempt estimates of reaction rates for very unstable (and as of yet unmeasured) nuclei along the $r$-process path. Using different prescriptions of nuclear data far from stability can lead to dramatic differences in both the extent of the $r$-process and the final shape of the abundance pattern (e.g., Kratz et al. 1993, 1998; Wanao et al. 2004; Mumpower et al. 2016). We test the robustness of the ADM model results by repeating our calculations using nuclear data informed by the Duflo-Zuker (DZ; Duflo & Zuker 1995) and the Hartree-Fock-Bogoliubov (HFB; Goriely et al. 2009) mass models. We use theoretical reaction and decay rates recalculated to be consistent with each mass model and use HFB barrier heights for fission rates within this mass model as in Vassh et al. (2018). Figure 10 shows the results using the disk wind trajectory and three different nuclear mass models, using the Ret II abundance constraints. Although using DZ and HFB mass models results in ADM distributions with more low-$Y_e$ mass, the relative shape and magnitude of high-$Y_e$ material reflects our results found when using the FRDM2012 mass model.

5.3. The Low-$Y_e$ Component

As seen in Figure 10, the amount of predicted low-$Y_e$ ejecta mass varies with mass model. In contrast, Figure 9 displays little variation when using a mix of ejecta types or entropies. In Figure 11, we quantify the fraction of very low $Y_e$ mass that the ADM model predicts is ejected when applying nuclear and astrophysical variations across a range of actinide abundances. The DZ mass model tends to allow ~5% more very low $Y_e$ material than FRDM2012 since simulations using the DZ mass model does not produce the actinides as robustly as with FRDM2012 (Holmbeck et al. 2019). Similarly, material leaves the actinide region due to higher neutron-induced reaction flows at later times with the HFB mass model compared to when using FRDM2012, also producing a lower final actinide abundance. As a result, using HFB masses allows for ≤10% more low-$Y_e$ mass than when employing FRDM2012. Using a combination
of tidal and wind ejecta or a combination of entropies slightly boosts the allowed very low $Y_e$ mass; however, the astrophysical variations lie comfortably within uncertainties in the nuclear masses.

In summary, accounting for nuclear mass model variations, the very low $Y_e$ ejected mass fractions may be as high as 40% to account for most observations of actinides in $r$-process enhanced metal-poor stars. Our results are robust under changes to the nuclear physics, with a variation of the allowed low-$Y_e$ component of $\sim$10% of the total mass when considering variations to nuclear mass models or astrophysical environments.

6. THE GW170817 ASSOCIATED KILONOVA

A parameterized accretion disk trajectory—and the conclusions drawn from using this trajectory—is consistent with one possible description of NSM ejecta environments. However, these conclusions are not necessarily unique and could still be applicable for other astrophysical sites, such as collapsars. Here we test if the ADM model results agree with what has been inferred from the GW170817 associated kilonova (“SSS17a” or “AT 2017gfo”). This could offer another hint for NSMs as primary $r$-process sources of material in early small, emerging dwarf galaxies that gave rise to the $r$-process enhanced stars.

Cowperthwaite et al. (2017) proposed that the light curve AT2017gfo could only be explained by multiple components: a lanthanide-poor (“blue”) and lanthanide-rich (“red”) component. Inspired by this two-component model, we split our ADM model $Y_e$ distributions for Ret II into a blue and red component. We define the blue component as primarily producing limited-$r$ elements, extending over a range of $0.29 < Y_e \leq 0.45$ (recall Figure 3), and the red component consisting of the remaining material at $Y_e \geq 0.29$. Using these ranges, we find lanthanide mass fractions of $X_{\text{lan}} = 10^{-0.8}$ for the red and $X_{\text{lan}} = 10^{-3.8}$ for the blue components when using our ADM model. The mass ratio between these components is $m_{\text{red}}/m_{\text{blue}} = 1.7$.

Kasen et al. (2017) also invoke a two-component model to resemble AT 2017gfo, based on the high opacity of lanthanide elements that would produce an extended emission spectrum. For their models to agree with AT 2017gfo, a lanthanide-rich red kilonova would need to have a lanthanide mass fraction of $X_{\text{lan}} \sim 10^{-1.5}$, and the lanthanide-poor blue kilonova would need to have $X_{\text{lan}} \sim 10^{-4}$. The ejecta mass ratio they estimate between these components is $m_{\text{red}}/m_{\text{blue}} = 1.6$.

The lanthanide mass fractions extracted from our model are slightly larger than those found by Kasen et al. (2017). Our ADM simulations do not extend to iron-peak elements, which could be produced in higher-$Y_e$ regions during a NSM event. Adding a contribution from iron-peak ejecta could bring our lanthanide mass fractions into further agreement with results by Kasen et al. (2017). Overall, our results agree, despite our inherently different approaches.

7. CONCLUSIONS

Using elemental abundances of $r$-process enhanced metal-poor stars, we have constructed empirical $Y_e$ distributions describing the ejecta of $r$-process events through the ADM model. We find that the $r$-process abundance signatures of actinide-boost and actinide-deficient stars can likely originate from variations in $Y_e$ distribution of ejecta from the same type of astrophysical $r$-process event. Both observationally and in the ADM model results, there is no clear point or distinct set of conditions at which the actinide-boost activates. Rather, the smoothness of the distribution of observed actinide abundances correlates well with the smooth growth of the allowed very low $Y_e$ tail of our ADM ejecta mass distributions, as seen in Figures 6 and 11.

Most actinide enrichments of metal-poor $r$-process enhanced stars can be explained by an $r$-process source with a very neutron-rich fission-cycling component. We estimate this fission-cycling ejecta to be a non-dominant (10–30%) constituent of the $r$-process ejecta mass. All levels of limited-$r$ abundance with respect to the lanthanides in stars with $\log \epsilon(\text{Zr/Dy}) \leq 0.95$ can be straightforwardly accommodated within the same $r$-process source. For these stars, the lanthanide-poor component but which is rich in limited-$r$ elements, constitutes about 25–40% of the ejecta mass. This suggests
that the $r$-process material in these stars need only come from one site that can produce the entire observed relative $r$-process abundance range from Sr to U.

The $r$-process signatures of very metal-poor stars allow the study of single $r$-process events, which we have characterized through the ADM model. We compared our empirically found progenitor $Y_e$ distributions of ejecta to the results of an independent study of the currently favored $r$-process site, an NSM. We found that both the lanthanide mass fraction and the red-to-blue mass ejecta ratio derived from the ADM model are consistent with results matching the light curve of the GW170817 associated kilonova, AT 2017gfo. The shape of our empirical $Y_e$ distributions also resemble those extracted from available hydrodynamical NSM simulations (Fernández et al. 2015; Radice et al. 2018). However, the accretion disk wind used in this work may be theoretically similar to—or perhaps even observationally indistinguishable from—other astrophysical sites, e.g., the accretion disk wind from a collapsar remnant. Future LIGO/aLIGO detections of NSMs and follow-up observations of their electromagnetic counterparts will be helpful to further characterize the progenitor site(s) of $r$-process enhanced stars.

In addition to investigations of NSMs and other $r$-process events, a comprehensive study of the $r$-process calls for more observations of metal-poor stars enhanced in these elements. Further identifications of $r$-II stars and their elemental abundances can be used to progress several areas of $r$-process studies. For example, more measurements of Th can test if DES J033523–540407 in Ret II and J0954+5246 in the halo represent limits on Th/Dy production, or if an even broader range exists. Large actinide variations at higher metallicities could indicate activity by other $r$-process sources as a function of chemical evolution, which can be identified and characterized through theoretical tools such as ADM. Detailed spectroscopy of more $r$-II stars will also allow further measurements of U. Due to the observed spread in abundance ratios, there is currently no unifying set of actinide-to-lanthanide production ratios that can be unilaterally applied to carry out cosmochronometry. However, the $U/Th$ ratio principally remains a robust and reliable tool for radioactive decay dating if ejecta distributions built from observed element patterns could be used to refine the required type of production ratios that accurately reflect the relevant progenitor site(s).

Overall, larger numbers of known $r$-II stars would increase e.g., identifications of kinematic groups in the Galactic halo or enable additional Th and U measurements. Hence, a main objective of the $R$-Process Alliance (RPA; Hansen et al. 2018; Sakari et al. 2018; Aprahamian et al. 2018) is to increase the number of known $r$-II stars from $\sim 30$ to $\sim 100$. Applying information from additional statistically significant kinematic groupings to the ADM model could then be used to investigate whether NSMs are main sources of $r$-process material, or if the ADM suggests that other $r$-process sources are predominantly needed.

The wealth of stellar abundance data—from surveys such as that being conducted by the RPA—together with theoretical $r$-process studies, future NSM detections, and nuclear physics constraints from next-generation rare-isotope beam facilities (e.g., FRIB) will allow thorough investigations of the origins of all $r$-process elements.

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